About of the determinant König-Egerváry graphs with a perfect matching

Gonzalo Molina

Universidad Nacional de San Luis, Argentina lgmolina@unsl.edu.ar

Kőnig-Egerváry graphs were introduced in [1]. They are graphs where the covering number equals the matching number. There exists a rich literature on the topic; see, for example, [2] and [3]. Graphs with (a unique) perfect matching have been extensively studied in the literature, see for example [4] and [5]. Harary in 1962, [see [6]], and Sachs in 1964, see [7], introduced what are now known as Sachs subgraphs, which consist of subgraphs where all components are edges or cycles.

In this work, it is proved, vía the notion of posy intorduced by Deming in [1], that every Kőnig-Egerváry graph with a perfect matching has a spanning bipartite graph with the same set of Sachs subgraphs, and therefore the same determinant.

Trabajo en conjunto con Daniel A. Jaume (Universidad Nacional de San Luis).

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